Standard Deviation and Normal Distribution

In many naturally occurring data sets, a histogram of the data is often bell shaped. In statistics, such data sets are said to have a **normal distribution**.

Standard Deviation and a Normal Distribution A normal distribution is symmetrical about its mean. 68.2% (about two-thirds) of the data lie within 1 standard deviation of the mean. 95.4% of the data lie within 2 standard deviations of the mean. 34.1% 34.1% 2.2% 2.2% 0.1% 0.1% 13.6% 13.6% 2 SD 4 SD 3 SD 1 SD 1 SD 2 SD Mean 3 SD 4 SD

EXAMPLE 3

Analyzing a Famous Normal Distribution

A famous data set was collected in Scotland in the mid-1800s. It contains the chest sizes (in inches) of 5738 men in the Scottish Militia. What percent of the chest sizes lie within 1 standard deviation of the mean?



The Thin Red Line is a painting by Robert Gibb. It was painted in 1881. Only the left portion of the painting is shown above.

Chest Size	Number of Men
33	3
34	18
35	81
36	185
37	420
38	749
39	1073
40	1079
41	934
42	658
43	370
44	92
45	50
46	21
47	4
48	1



SOLUTION

The number of chest sizes within 1 standard deviation of the mean is 749 + 1073 + 1079 + 934 + 658 = 4493. This is about 78.3% of the total, which is somewhat more than the percent predicted by a normal distribution.



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What percent of the chest sizes lie within 2 standard deviations of the mean?