Study Tip

In mathematics, numbers in a sequence are often denoted by letters with subscripts. For instance, the numbers in an exponential growth sequence can be denoted by

 $A_0, A_1, A_2, \dots, A_{n-1}, A_n.$ A_0 is read as "A sub zero."

Finding an Exponential Growth Rate

Exponential Growth Rate

If A_0 and A_1 are the quantities for any two times, then the growth rate between those times, *r*, is given by

 $\frac{A_1}{A_0} = 1 + r.$

EXAMPLE 5

Finding an Exponential Growth Rate

You purchase 100 shares of a stock for \$4.35 per share. One month later, the value of the stock is \$4.55 per share.

- **a. Linear Growth:** The value of the stock continues to increase by the *same dollar amount* each month. How much will your investment be worth in 2 years?
- **b.** Exponential Growth: The value of the stock continues to increase by the *same percent* each month. How much will your investment be worth in 2 years?

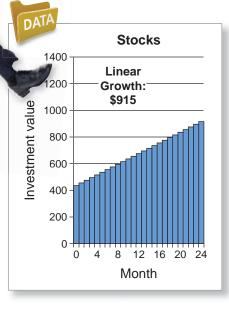
 $\frac{4.55}{4.35} \approx 1.046$

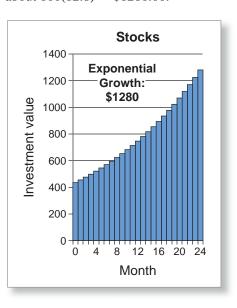
SOLUTION

a. Linear Growth: If the stock continues to increase by \$0.20 per month, each share will be worth 4.35 + 24(0.2) = \$9.15. So, your investment will be worth

100(9.15) = \$915.00.

b. Exponential Growth: The rate of growth from \$4.35 to \$4.55 is about 4.6%. If the stock continues to grow at this rate, in 2 years each share will be worth $4.35(1.046)^{24} = 12.80 . So, your investment will be worth about 100(12.8) = \$1280.00.





✓ Checkpoint

Help at Math.andYOU.com

Using each type of growth, how much will the stock be worth in 4 years? Illustrate each type with a graph.